

Global Stability of a Generalized Cohen-Grossberg Model with Unbounded Time-Varying Delays

Teresa Faria^a and José J. Oliveira^b

^aDepartamento de Matemática and CMAF, Faculdade de Ciências,
Universidade de Lisboa, Campo Grande, 1749-016 Lisboa, Portugal
e-mail: tfaria@ptmat.fc.ul.pt

^bDepartamento de Matemática and CMAT, Escola de Ciências,
Universidade do Minho, Campus de Gualtar, 4710-057 Braga, Portugal
e-mail: jjoliveira@math.uminho.pt

Abstract

In this talk, we establish sufficient conditions for the existence and global stability of an equilibrium point of the following generalized Cohen-Grossberg neural network model with unbounded discrete time-varying delays:

$$\dot{x}_i(t) = -k_i(x_i(t)) \left(b_i(x_i(t)) + \sum_{j=1}^n \sum_{p=1}^P h_{ij}^{(p)}(x_j(t - \tau_{ij}^{(p)}(t))) \right), t \geq 0, \quad (1)$$

where $k_i, h_{ij}^{(p)}, \tau_{ij}^{(p)} : \mathbb{R} \rightarrow \mathbb{R}$ are continuous with $k_i(t), \tau_{ij}^{(p)}(t)$ positive.

We apply the results to the particular model

$$\dot{x}_i(t) = -k_i(x_i(t)) \left[b_i(x_i(t)) - \sum_{j=1}^n c_{ij} g_j(x_j(t)) - \sum_{j=1}^n d_{ij} f_j(x_j(t - \tau_{ij}(t))) \right], \quad (2)$$

improving recent results in the literature.

We emphasize that, contrary to the usual, we do not use Lyapunov functionals to obtain our results.